Background
Light and the interaction of light and matter is governed by the rules of quantum electrodynamics. When the photon densities are so too high that electrons are accelerated to relativistic speeds (as occurs at the highest laboratory laser fields), the rules of quantum mechanics can be used. We start here.

QM description: \[ E = h\nu \]. One- and multi-photon transition cross-sections \( \delta E \delta t = h \). Uncertainty and lifetimes \( (h \equiv \text{Plank's constant}) \).

Wave description: \( \nu = c/\lambda \). Diffraction and interference effects.
\[ \delta \lambda/\lambda = \lambda/L_{\text{coh}} \text{ or } L_{\text{coh}} = \lambda^2/(\delta \lambda)^2 \]. Spatial coherence effects.
\[ \delta \theta \delta a = \lambda \]. Uncertainty between angular spread and size of beam.

Geometric optics: \( \lambda \to 0 \), so that diffraction is ignored and the resolution angle, \( \lambda/(\text{size of system}) \) goes to zero as well. Light is described by rays.

Paraxial optics: \( \delta \lambda/\lambda \approx 0 \), \( \partial[z]/\partial z \ll \partial[z]/\partial r \). Only small angles, so that imaging design is in terms of straight lines and two parameters, the height of a ray and the slope of the ray.

Matrix method for rays: We start with a notation for specifying optics systems.
\[ z \] axial location of a ray.
\[ r_1 \] height of a ray at axial location \( z_1 \).
\[ r'_1 \] slope of a ray at axial location \( z_1 \), \( i.e., r' = \partial r/\partial z \).

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1 \( E = h\nu = 1.24/\lambda \) eV with \( \lambda \) in micrometers, so that blue light is 3 eV, red light is 2 eV.
2 Noting that \( \delta \lambda = c \delta t \), \( L_{\text{coh}} = \lambda^2/(c \delta t) \approx (0.8 \mu m)^2/(3 \times 10^{14} \mu m/s \cdot 1 \times 10^{-13} s) = 2 \mu m \) for 2-photon excitation.
\( n_1 \) optical index at axial location \( z_1 \).
\( d \) separation distances along axial axis.
\( R \) radius of curvature of a spherical lens.
\( f \) focal length (function of \( n \) and \( R \) at each interface); we will show that \( f = R/(n-1) \) for a thin planoconvex lens.

Formalism to connect rays at two locations. General idea:

- Two unknowns requires two equations.

\[
\begin{pmatrix} r_2 \\ r'_2 \end{pmatrix} = \begin{pmatrix} Ar_1 + Br'_1 \\ Cr_1 + Dr'_1 \end{pmatrix} = \begin{pmatrix} A & B \\ C & D \end{pmatrix} \begin{pmatrix} r_1 \\ r'_1 \end{pmatrix} = T \begin{pmatrix} r_1 \\ r'_1 \end{pmatrix}
\]

- Represent each interface or transition by an appropriate ABCD, or transfer matrix. Then whole optical systems are reduced to a single matrix by multiplying through matrices for each component. We recall that matrix algebra involves

\[
T \cdot t = \begin{pmatrix} A & B \\ C & D \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} = \begin{pmatrix} Aa + Bc & Ab + Bd \\ Ca + Dc &Cb + Dd \end{pmatrix}.
\]

- Ignore reflections – consider only “forward” propagation, so that amplitudes are constant.

Just to complete the story, an extension of this formalism also holds for beams with a Gaussian profile, in which \( r \) is replaced by a complex variable that describes the width and curvature of the bean (see Yariv).

**Propagation through space.** We start with a ray that propagates a distance \( d \) in space with constant index.

- The slope will remain unchanged.
- The height will change by the slope times the distance.
We have \( \begin{pmatrix} r_2' \\ r_2 \\ \end{pmatrix} = \begin{pmatrix} r_1 + dr_1' \\ 0r_1 + r_1' \\ \end{pmatrix} = \begin{pmatrix} 1 & d \\ 0 & 1 \\ \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \\ \end{pmatrix} \), so the matrix for propagating a distance \( d \) is

\[
T_{\text{prop}} = \begin{pmatrix} 1 & d \\ 0 & 1 \\ \end{pmatrix}.
\]

**Snells’ Law.** Before we can move on to rays that impinge on an interface, we need to recall Snell’s law – which describes the angle of the transmitted ray. A derivation in terms of minimizing the time to travel between two points is given in appendix A. We consider a ray that propagates from a material with index \( n_1 \) to one with index \( n_2 \). The ray is incident at an angle \( \theta_1 \) relative to the normal to the interface. Snells’ law relates the exit angle, \( \theta_2 \), to the indices and entrance angle by \( n_1 \sin \theta_1 = n_2 \sin \theta_2 \).

![Snells' Law Diagram](image)

**Flat interface.** We move on to an interface with index \( n_1 \) to the left and \( n_2 \) to the right.

- In the paraxial approximation, \( r' = \tan \theta = \sin \theta \), so that Snells’ law becomes
  
  \( n_1 r'_1 = n_2 r'_2 \).

- Since \( r_1 = r_2 \) at the interface, \( \begin{pmatrix} r_2' \\ r_2' \\ \end{pmatrix} = \begin{pmatrix} r_1 + 0r_1' \\ 0r_1 + \frac{n_1}{n_2}r_1' \\ \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & \frac{n_1}{n_2} \\ \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \\ \end{pmatrix} \)

Thus the matrix for propagating across the interface is

\[
T_{\text{flat}} = \begin{pmatrix} 1 & 0 \\ 0 & \frac{n_1}{n_2} \\ \end{pmatrix}.
\]

**Example: Propagation through a slab of thickness \( d \).** This gives us a first nontrivial example to compute the propagation of a ray. We start on the right and consider the interface from \( n_1 \) to \( n_2 \) and then back to \( n_1 \) again.
The relationship between the input and the output is:

\[
\begin{pmatrix} r_4 \\ r'_4 \end{pmatrix} = \mathbf{T}_{\text{flat} \cdot \mathbf{T}_{\text{prop} \cdot \mathbf{T}_{\text{flat} \cdot \mathbf{T}_{r_1'}}} = \begin{pmatrix} 1 & 0 \\ 0 & \frac{n_2}{n_1} \end{pmatrix} \begin{pmatrix} 1 & d \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & \frac{n_1}{n_2} \end{pmatrix} \begin{pmatrix} r_1 \\ r'_1 \end{pmatrix} = \begin{pmatrix} 1 & d \frac{n_1}{n_2} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} r_1 \\ r'_1 \end{pmatrix}
\]

Note the ordering of the transfer matrices – which is right to left! The final matrix, \( \begin{pmatrix} 1 & d \frac{n_1}{n_2} \\ 0 & 1 \end{pmatrix} \), looks just like the free propagator, except that the distance is normalized by \( n_1/n_2 \).\(^3\) The position is displaced, but the entrance and exit angles remain unchanged.

**Spherical Interface.** We now come to propagation through a curved interface, which is the first step in understanding a lens. We derive the transfer matrix in a general way.

The beam enters and leaves the interface at height

- \( r_1 = r_2 = r \).

All angles are all taken to be small

\(^3\) This rescaling is also a statement that the wavelength of light changes with the index.
• The normal to the surface makes an angle \( \sin(r/R) \approx r/R \).
• The slopes are small, so that \( \tan(r_1') \approx r_1' \) and \( \tan(r_2') \approx r_2' \).
• From Snell's law at small angles, \( n_1 \theta_1 \approx n_2 \theta_2 \) or \( n_1 (r_1' + r/R) = n_2 [r/R - (-r_2')] \).
• Thus \( r_2' = (n_1/n_2 - 1)(r/R) + (n_1/n_2)r_1' \) so that \( \begin{pmatrix} r_2' \\ r_2 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ n_1/n_2 & 1 \\ R_1/R_2 & n_2/n_1 \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \end{pmatrix} \).

\[ T_{\text{curved}} = \begin{pmatrix} 1 & 0 \\ n_1/n_2 & 1 \\ R_1/R_2 & n_2/n_1 \end{pmatrix}. \]

In the limit that \( R \to \infty \) we recover our result for the flat surface.

**Lens.** The most general lens involves a change in index through a curved surface of radius \( R_1 \), propagation through the lens material, and exit through a second curved surface of radius \( R_2 \). We save this general case for Appendix B, and consider the special but useful case of a thin lens that is curved on the left side with radius of curvature \( R_1 \) and on the right side with radius of curvature \( R_2 \). From the above result,

• The indices at the entrance side and exit side are identical, *i.e.*, \( n_1 \), while the index in the lens is \( n_2 \).

\[ \begin{pmatrix} r_3 \\ r_3' \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ n_2/n_1 & 1 \\ R_2/R_1 & n_1/n_2 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ n_1/n_2 & 1 \\ R_1/R_2 & n_2/n_1 \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ n_2/n_1 & 1 \\ R_2/R_1 & n_1/n_2 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ R_1/R_2 & n_2/n_1 \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \end{pmatrix}. \]

• We define the focal length, denoted \( f \), is defined through

\[ \frac{1}{f} = \frac{n_2/n_1}{1/R_1 - 1/R_2} \]

where \( R \) is positive for a convex surface (of particular relevance in microscopy) and negative for a concave surface. For a symmetric biconvex lens, \( R_2 = -R_1 \). For a planoconvex lens, \( R_2 \to \infty \).

\[ T_{\text{thin lens}} = \begin{pmatrix} 1 & 0 \\ -1/f & 1 \end{pmatrix}. \]

**Imaging (at last!).** We now consider three classic configurations of lenses.

**Space-lens-space.** A ray starts a distance \( d_1 \) from a thin lens and is observed a distance \( d_2 \) away.
Thus \[
\begin{pmatrix}
 r_2 \\
 r'_2
\end{pmatrix} = \begin{pmatrix}
 1 & d_2 \\
 0 & 1
\end{pmatrix} \begin{pmatrix}
 1 & 0 \\
 -\frac{1}{f} & 1
\end{pmatrix} \begin{pmatrix}
 1 & d_1 \\
 0 & 1
\end{pmatrix} \begin{pmatrix}
 r_1 \\
 r'_1
\end{pmatrix} = \left( 1 - \frac{d_2}{f} \frac{d_1 + 1}{d_1 - \frac{d_2}{f}} \right) \begin{pmatrix}
 r_1 \\
 r'_1
\end{pmatrix}
\]

\[
T_{s-l-s}' = \begin{pmatrix}
 1 - \frac{d_2}{f} & d_1 + \frac{d_2}{f} \\
 -\frac{1}{f} & 1 - \frac{d_1}{f}
\end{pmatrix}. 
\]

- **Imaging condition.** This corresponds to a final height, \( r_2 \), that is independent of initial slope, \( i.e. \), \( r'_1 \), so that all rays that leave \( r_1 \) converge at \( r_2 \). Thus the “B” term of the transfer matrix must be zero, \( i.e. \), \( d_1 + d_2 - (d_1 d_2)/f = 0 \). This leads to the famous lens formula

\[
\frac{1}{d_1} + \frac{1}{d_2} = \frac{1}{f}
\]

- **Magnification.** When the imaging condition is satisfied, the “A” term corresponds to magnification, \( i.e. \), \( r_2 = [1-(d_2/f)] r_1 = -(d_2/d_1) r_1 \) where the minus sign means the image is inverted.

\[
\frac{r_2}{r_1} = -\frac{d_2}{d_1}
\]

- **Real vs. Virtual.** Note that for the case of \( d, < f \), the lens formula implies that \( d_2 < 0 \) and thus the sign of the magnification is now positive. Therefore, an upright image is formed to the left of the lens. There is no image to project on a screen. However, the upright image can form the object for another lens.

- **Ray tracing rules.** The imaging condition leads to a transfer matrix that can be written in three equivalent forms:

\[
T_{s-l-s} \rightarrow \begin{pmatrix}
 \frac{-f}{d_1 - f} & 0 \\
 \frac{-1}{f} & \frac{-d_2 - f}{d_2 - f}
\end{pmatrix} = \begin{pmatrix}
 \frac{-d_2}{d_1} & 0 \\
 \frac{-1}{f} & \frac{-f}{d_2 - f}
\end{pmatrix} = \begin{pmatrix}
 \frac{-d_2}{d_1} & 0 \\
 \frac{-1}{d_1} + \frac{1}{d_2} & \frac{-f}{d_2 - f}
\end{pmatrix}.
\]

Each of these forms leads to one of three ray-tracing rules:
1. Consider a horizontal ray from the “object”, \( r'_{1} = 0 \):

\[
\begin{pmatrix}
  r_2 \\
  r'_2
\end{pmatrix} = \begin{pmatrix}
  -\frac{d_2-f}{t} & 0 \\
  -\frac{1}{t} & -\frac{f}{d_2-f}
\end{pmatrix} \begin{pmatrix}
  r_1 \\
  0
\end{pmatrix} = \begin{pmatrix}
  -\frac{d_2-f}{t} r_1 \\
  -\frac{1}{t} r_1
\end{pmatrix}.
\]

The output ray will cross the axis at \( d_2 = f \), the right focal point of the lens, and is imaged at

\[
\begin{pmatrix}
  r_2 \\
  r'_2
\end{pmatrix} = \begin{pmatrix}
  -\frac{d_2-f}{t} r_1 \\
  -\frac{1}{t} r_1
\end{pmatrix} = \begin{pmatrix}
  -\frac{d_2}{d_1} r_1 \\
  -\frac{r_1}{d_1}
\end{pmatrix}.
\]

2. Consider a ray from the “object” to the center of the lens, \( i.e., r'_{1} = -r_1/d_1 \):

\[
\begin{pmatrix}
  r_2 \\
  r'_2
\end{pmatrix} = \begin{pmatrix}
  -\frac{d_2}{d_1} & 0 \\
  -\frac{1}{d_1 + \frac{1}{d_2}} & -\frac{1}{d_1}
\end{pmatrix} \begin{pmatrix}
  r_1 \\
  r_1/d_1
\end{pmatrix} = \begin{pmatrix}
  -\frac{d_2}{d_1} r_1 \\
  -\frac{r_1}{d_1}
\end{pmatrix}.
\]

The output ray has a slope that is unchanged.

3. Consider a ray from the “object” that passes through the left focal point, \( i.e., r'_{1} = -r_1/(d_1-f) \)

\[
\begin{pmatrix}
  r_2 \\
  r'_2
\end{pmatrix} = \begin{pmatrix}
  -\frac{f}{d_1-f} & 0 \\
  -\frac{1}{t} & -\frac{d_1-f}{t}
\end{pmatrix} \begin{pmatrix}
  r_1 \\
  -\frac{r_1}{d_1-f}
\end{pmatrix} = \begin{pmatrix}
  -\frac{d_2}{d_1} r_1 \\
  0
\end{pmatrix}.
\]

The output ray has a slope that is now zero.

These three rays will converge at a common point, \( d_2 = (fd_1)/(d_1-f) \), as given by the imaging condition.

**Lens-space-lens.** A ray enters one thin lens, travels a distance \( d \), and then exits through a second thin lens.
Thus \( \mathbf{r} = \left( \begin{array}{c} r_2 \\ r_2' \end{array} \right) = \left( \begin{array}{cc} 1 & 0 \\ -\frac{1}{f_2} & 1 \end{array} \right) \left( \begin{array}{cc} 1 & d \\ 0 & 1 \end{array} \right) \left( \begin{array}{c} r_1 \\ r_1' \end{array} \right) = \left( \begin{array}{cc} 1 - \frac{d}{f_1} & d \\ \frac{d-f_1 r_2}{f_1 f_2} & 1 - \frac{d}{f_2} \end{array} \right) \left( \begin{array}{c} r_1 \\ r_1' \end{array} \right) \)

\[
\mathbf{T}_{l-s-l} = \left( \begin{array}{cc} 1 - \frac{d}{f_1} & d \\ \frac{d-f_1 r_2}{f_1 f_2} & 1 - \frac{d}{f_2} \end{array} \right).
\]

- **Back-to-back lenses.** We let \( d \to 0 \) and the transfer matrix becomes

\[
\mathbf{T}_{l-s-l} \to \left( \begin{array}{cc} 1 & 0 \\ -\frac{1}{f_1 + f_2} & 1 \end{array} \right)
\]

Thus the composite lens has an effective focal length equal to the geometric mean of the focal length of the two lenses, *i.e.*, \( \frac{1}{f_{\text{effective}}} = \frac{1}{f_1} + \frac{1}{f_2} \).

- **Beam expander.** This corresponds to the case of collimated output, for which the slope \( r_2' \) is independent of \( r_1 \). Thus the “C” term in \( \mathbf{T}_{l-s-l} \) must be equal to zero, *i.e.*, \( d - f_1 - f_2 = 0 \). This leads to the famous telescope formula:

\[
d = f_1 + f_2
\]

which can be used to change the height of parallel light by \( \frac{r_2}{r_1} = \frac{f_2}{f_1} \). The transfer matrix becomes:

\[
\mathbf{T}_{l-s-l} \to \left( \begin{array}{cc} -\frac{f_2}{f_1} & f_1 + f_2 \\ 0 & -\frac{f_2}{f_2} \end{array} \right).
\]
Imager/Scanner. The above analysis provides an introduction to scanning. This corresponds to a secession of 7 matrices that are put together in the sequence from a scan mirror to a sample:

\[
\begin{pmatrix}
  r_4 \\
  r'_4
\end{pmatrix} = \begin{pmatrix} 1 & d_3 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \tfrac{1}{f_1} & 1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \tfrac{1}{f_2} & 1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \tfrac{1}{f_3} & 1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & d_2 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & d_1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} r_i \\ r'_i \end{pmatrix}
\]

To simply greatly, we consider the particular (and relevant) case of \( d_1 = f_1, d_2 = f_1 + f_2, d_3 = f_2, \) and \( d_4 = f_3 \), so that the above sequence reduces to:

\[
\begin{pmatrix}
  r_4 \\
  r'_4
\end{pmatrix} = \begin{pmatrix} 1 & f_3 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \tfrac{1}{f_1} & 1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \tfrac{1}{f_2} & 1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & f_1 + f_2 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & f_1 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} r_i \\ r'_i \end{pmatrix}
\]

\[
= \begin{pmatrix} 0 & -f_3 \frac{f_1}{f_2} \\ \frac{1}{f_2} \cdot \frac{1}{f_3} & -1 \end{pmatrix} \cdot \begin{pmatrix} r_i \\ r'_i \end{pmatrix}
\]

The critical point is that a change in the initial slope is turned into a change solely in position of the beam in the object plane, i.e.,

\[
r_4 = -f_3 \frac{f_1}{f_2} r'_i.
\]

\(^4\) Objectives are usually specified by magnification, denoted \( M \), e.g., \( M = 40 \) for a 40-X lens, rather than their focal length, \( f_3 \), in the above notation. The correspondence makes use of an assumed image distance, denoted \( L \). Equivalently, the objective may have the image projected to infinity, but the tube lens brings it to focus at a distance \( L \) from the tube lens. We have \( M = \frac{L}{d_4} \) and \( \frac{1}{L} \cdot \frac{1}{d_4} = \frac{1}{f_3} \) for \( f_3 = \frac{L}{M+1} \).

For example, for typical values \( L = 160 \text{ mm} \) and \( M = 40 \), the focal length is \( f_3 = 4 \text{ mm} \).
This is the essence of scanning, as the slope is set by the angle of the mirrors whose manipulation is under control of a galvanometer. By the way, the maximum scan angle \( r_1' \) is related to the field of view \( (2 \times r_4) \) by 

\[
\text{Max scan angle} = \frac{\text{field of view}}{2 \cdot f_{\text{scan}}} \cdot \frac{f_{\text{lube}}}{f_{\text{objective}}} = \frac{\text{field of view}}{2 \cdot f_{\text{scan}}} (M+1)
\]

in radians, or \( \sim 4^\circ \) for a typical system. Note the intermediate result for the image of the mirrors at the back of the objective, i.e.,

\[
\begin{pmatrix} r_3 \\ r_3' \end{pmatrix} = \begin{pmatrix} 1 & f_2 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -\frac{1}{f_2} & 1 \end{pmatrix} \begin{pmatrix} 1 & f_i + f_2 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -\frac{1}{f_1} & 1 \end{pmatrix} \begin{pmatrix} 1 & f_i \\ 0 & 1 \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \end{pmatrix}
\]

\[
= \begin{pmatrix} -\frac{f_2}{r_1} & 0 \\ 0 & -\frac{f_i}{r_1} \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \end{pmatrix},
\]

which says that the mirrors are in focus at the entrance of the objective, since the final height is independent of the initial slope. Further, the diameter of the (laser) beam at the objective is related to the diameter of the incident (laser) beam by

\[
\text{Beam diameter at objective} = \frac{f_{\text{lube}}}{f_{\text{scan}}} \cdot \text{Beam diameter at mirror}.
\]

This ratio is chose to insure that the aperture of the objective is filled. While we have not discussed issues of resolving power in this talk, since we let \( \lambda \rightarrow 0 \) for purposes of ray tracing, filling the aperture insures that we utilize the full resolving power of the objective, i.e.,

\[
\text{Minimum resolution} \sim \lambda \cdot \frac{\text{focal length of objective}}{\text{diameter of objective}}
\]
Appendix A - Derivation of Snell’s Law based on principle of minimum time

Distances
\[ d_1 = \sqrt{(x - x_i)^2 + (y - y_i)^2} \]
\[ d_2 = \sqrt{(x_f - x)^2 + (y_f - y)^2} \]

Speeds
\( v_1 = \frac{c}{n_1} \)
\( v_2 = \frac{c}{n_2} \)

Calculate the total time of transit, \( T \).
\[ T = \frac{d_1}{v_1} + \frac{d_2}{v_2} = \frac{n_1}{c} \sqrt{(x - x_i)^2 + (y - y_i)^2} + \frac{n_2}{c} \sqrt{(x_f - x)^2 + (y_f - y)^2} \]

Take the derivative of the total transit time with respect to the position, \( x \). As we are interested at the contact point at the plane of the interface, we set \( y = 0 \).
\[ \frac{dT}{dx}\bigg|_{y=0} = \frac{n_1}{c} \frac{2(x - x_i)}{\sqrt{(x - x_i)^2 + (y - y_i)^2}} - \frac{n_2}{c} \frac{2(x_f - x)}{\sqrt{(x_f - x)^2 + (y_f - y)^2}} \]
\[ = \frac{n_1}{c} 2 \sin(\theta_1) - \frac{n_2}{c} 2 \sin(\theta_2) \]

The total transit time is minimized when \( dT/dx|_{y=0} = 0 \). This leads to the identity
\[ n_1 \sin \theta_1 = n_2 \sin \theta_2 \]

Appendix B

Coming soon – still!