

14 The centripetal acceleration is

$$a_c = r\omega^2, \text{ where } r = \frac{d}{2} = \frac{1}{2}(5 \text{ mi}) = \frac{5}{2}(1609 \text{ m})$$

\therefore we want $a_c = g$

$$\therefore \omega = \sqrt{\frac{a_c}{r}} = \sqrt{\frac{2g}{d}} = \sqrt{\frac{9.8 \text{ m/s}^2 \times 2}{5(1609 \text{ m})}} = \boxed{0.05 \text{ rad/s}}$$

17 The angular velocity of the disk 3.0 s after starting from rest is:

$$\omega = 78 \frac{\text{rev}}{\text{min}} \left(\frac{2\pi \text{ rad}}{1 \text{ rev}} \right) \left(\frac{1 \text{ min}}{60 \text{ s}} \right) = 8.2 \text{ rad/s}$$

and the bug follows a circular path of radius

$$r = 5.0 \text{ m} \left(\frac{1 \text{ m}}{3\pi \cdot 37 \text{ m}} \right) = 0.13 \text{ m}$$

(a) The constant angular acceleration of the disk is

$$\alpha = \frac{\omega - \omega_0}{t} = \frac{8.2 \text{ rad/s} - 0}{3.0 \text{ s}} = 2.7 \text{ rad/s}^2$$

The tangential acceleration of the bug is $a_t = r\alpha$,

$$\text{thus } a_t = (0.13 \text{ m})(2.7 \text{ rad/s}^2) = \boxed{0.35 \text{ m/s}^2}$$

(b) When the disk is rotating at its final angular velocity, $\omega = 8.2 \text{ rad/s}$, and

$$v_t = r\omega = (0.13 \text{ m})(8.2 \text{ rad/s}) = \boxed{1.0 \text{ m/s}}$$

(c) Since both r and α are constant, the tangential acceleration, $a_t = r\alpha$, is also constant. Thus

$$\text{at } t = 1.0 \text{ s}, a_t = \boxed{0.35 \text{ m/s}^2}$$

The tangential velocity of the bug is

$$v_t = (v_t)_{t=0} + at = 0 + (0.35 \text{ m/s}^2)(1.0 \text{ s}) = 0.35 \text{ m/s}$$

and the centripetal acceleration is

7.20 Since $F_c = m \frac{v_t^2}{r} = mr\omega^2$, the needed angular velocity is

$$\omega = \sqrt{\frac{F_c}{mr}} = \sqrt{\frac{4.0 \times 10^{-11} \text{ N}}{(3.0 \times 10^{-16} \text{ kg})(0.150 \text{ m})}}$$

$$= (9.4 \times 10^2 \text{ rad/s}) \left(\frac{1 \text{ rev}}{2\pi \text{ rad}} \right) = \boxed{1.5 \times 10^2 \text{ rev/s}}$$

7.22 $a_c = \frac{v_t^2}{r} = \frac{\left[\left(86.5 \frac{\text{km}}{\text{h}} \right) \left(\frac{1 \text{ h}}{3600 \text{ s}} \right) \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) \right]^2}{61.0 \text{ m}} \left(\frac{1 \text{ g}}{9.80 \text{ m/s}^2} \right) = \boxed{0.966 \text{ g}}$

7.35 (a) The gravitational force must supply the required centripetal acceleration, so

$$\frac{Gm_E m}{r^2} = m \left(\frac{v_t^2}{r} \right). \text{ This reduces to } r = \frac{Gm_E}{v_t^2}, \text{ which gives}$$

$$r = \left(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \right) \frac{(5.98 \times 10^{24} \text{ kg})}{(5000 \text{ m/s})^2} = 1.596 \times 10^7 \text{ m}.$$

The altitude above the surface of the Earth is then

$$h = r - R_E = 1.596 \times 10^7 \text{ m} - 6.38 \times 10^6 \text{ m} = \boxed{9.58 \times 10^6 \text{ m}}.$$

(b) The time required to complete one orbit is

$$T = \frac{\text{circumference of orbit}}{\text{orbital speed}} = \frac{2\pi(1.596 \times 10^7 \text{ m})}{5000 \text{ m/s}} = 2.00 \times 10^4 \text{ s} = \boxed{5.57 \text{ h}}.$$

37 Kepler's third law gives $T^2 = \left(\frac{4\pi^2}{GM_J} \right) r^3 \Rightarrow$

$$M_J = \frac{4\pi^2}{G} \frac{r^3}{T^2} = \frac{4(3.14)^2}{6.673 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2} \frac{(4.22 \times 10^5 \times 10^3 \text{ m})^3}{(1.77 \times 24 \times 3600 \text{ s})^2}$$

$$= \boxed{1.90 \times 10^{27} \text{ kg}}$$

38 (a) $PE = -G \frac{M_E m}{r}$ where $r = R_E + h \Rightarrow$

$$PE = -G \frac{M_E m}{R_E + h} = -6.673 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2 \frac{5.98 \times 10^{24} \text{ kg} (100 \text{ kg})}{6.38 \times 10^6 \text{ m} + 2 \times 10^6 \text{ m}}$$

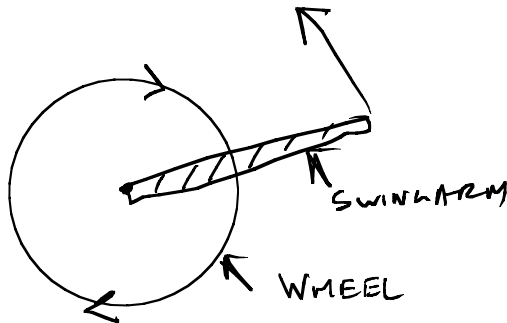
$$= \boxed{-4.76 \times 10^9 \text{ J}}$$

(b) $F = G \frac{M_E m}{r^2} = G \frac{M_E m}{(R_E + h)^2}$

$$= 6.673 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2 \frac{5.98 \times 10^{24} \text{ kg} (100 \text{ kg})}{(6.38 \times 10^6 \text{ m} + 2 \times 10^6 \text{ m})^2}$$

$$= \boxed{568 \text{ N}} \text{ toward the Earth.}$$

C71



IN ORDER TO CONSERVE ANGULAR MOMENTUM, AS THE SPEED OF THE WHEEL INCREASES, THE NOSE OF THE BIKE MUST LIFT.

C16)

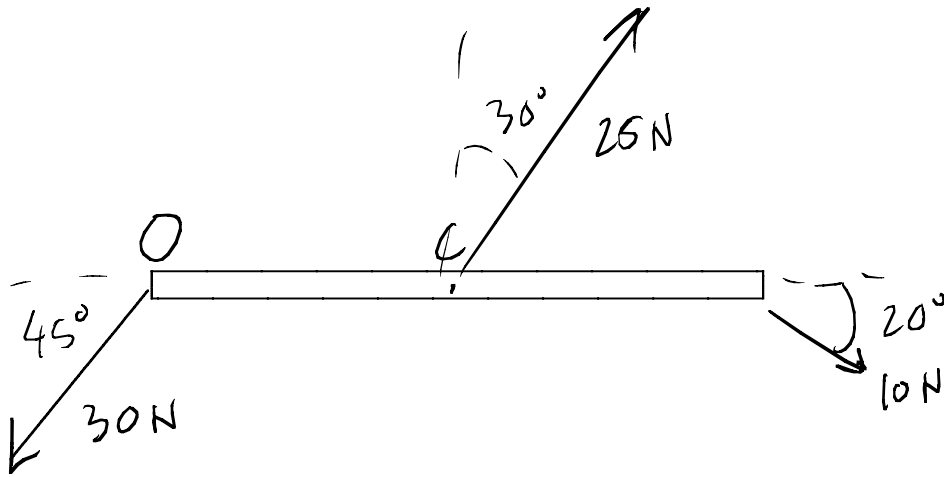
THIS QUESTION HAS 2 ANSWERS. THE CAT ROTATES TO CONSERVE ANGULAR MOMENTUM. THE RESULT MOTION IS SLIGHTLY COMPLICATED AND INVOLVES MULTIPLE STAGES. SEE ME

(BEN) IF YOU WANT A FULL EXPLANATION.

1] The magnitude of the torque $\vec{\tau}$ of the force \vec{F} is given by $\tau = rF \sin\theta$, where r is the length of the position vector, θ the angle between \vec{F} and \vec{r} . Thus, when $\theta = \frac{\pi}{2}$, F reaches its minimum value:

$$F_{\min} = \frac{\tau}{r \cdot \sin\theta} \Big|_{\theta = \frac{\pi}{2}} = \frac{40.0 \text{ N} \cdot \text{m}}{(30.0 \text{ cm}) \times 1} = \frac{40.0 \text{ N} \cdot \text{m}}{0.30 \text{ m}} = \boxed{133 \text{ N}}$$

8.3)



a.) Torque at C:

$$2.0 \text{ METERS} \cdot 25 \text{ N} \cdot \cos(30^\circ)$$

Torque at END:

$$-10 \text{ N} \cdot 4 \text{ METERS} \cdot \sin(20^\circ)$$

$$\text{Total: } 30 \text{ N} \cdot \text{m} \quad \odot$$

b.) Torque at O:

$$-30 \text{ N} \cdot -2 \text{ m} \cdot \sin 45$$

Torque at END:

$$2.0 \cdot -10 \text{ N} \cdot \sin 20^\circ$$

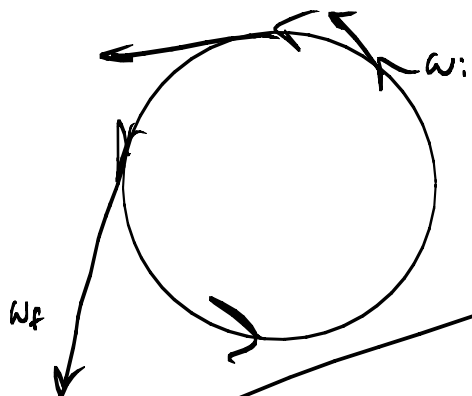
$$\text{Total: } 36 \text{ N} \quad \odot$$

HOMEWORK APPENDUM - Week 8

Note Title

3/6/2006

13.)



$$37 \text{ rev.} \cdot 2\pi = \Delta\theta$$

$$t = 3.0 \text{ s}$$

$$\omega_f = 98.0 \text{ r/s}$$

$$\omega_f^2 = \omega_i^2 + 2\alpha(\Delta\theta)$$

$$\omega_f = \omega_i + \alpha t$$

$$\omega_i = \omega_f - \alpha t$$

$$\omega_f^2 = \omega_f^2 - 2\omega_f \alpha t + \alpha^2 t^2 + 2\alpha(\Delta\theta)$$

$$\alpha^2 t^2 + \alpha(\Delta\theta \cdot 2 - 2\omega_f t) = 0$$

$$\alpha[\alpha t^2 + 2\Delta\theta - 2\omega_f t] = 0$$

TRIVIAL SOLUTION $\alpha = 0$

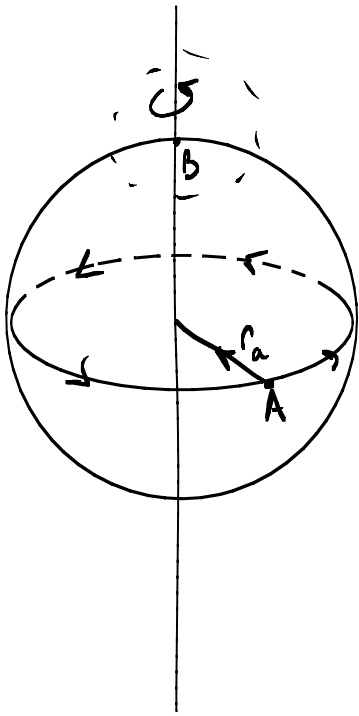
NON TRIVIAL:

$$\alpha = \frac{2[\omega_f t - \Delta\theta]}{t^2} = \frac{2[98 \text{ r/s} \cdot 3 \text{ s} - 37 \cdot 2\pi \text{ rad}]}{3.0 \text{ s}^2}$$

$$= 13.7 \text{ r/s}^2$$

UNITS MAKE SENSE.

16.)



$$A: a_c = \frac{v^2}{r_a} =$$

$$r_{\text{earth}} = 6378 \text{ km}$$

$$1 \text{ day} = 2\pi = 24 \text{ hours} = 86400$$

$$v_{\text{EQUATOR}} = \frac{2\pi r_e}{T} = 465 \text{ m/s}$$

$$a_c = \frac{v^2}{r_a} = 3.3 \times 10^{-2} \frac{\text{m}}{\text{s}^2} \text{ INWARD.}$$

b.) \nearrow

THE NORTH POLE, THIS IS EASY.

$$v = \frac{2\pi r_a}{T} = 0, \quad \text{so } a_c = 0.$$