

W20 PHYS 178/278 Final Project Logistics

- **Team up**

You are going to forming a team, ideally of two, for working on a project together.

The project sign-up sheet will be emailed to you.

- **Topics**

You may choose a project from the suggested topics lists or bring up one that interests you or is relevant to your ongoing research.

The references of suggested topics are available here:

<https://www.dropbox.com/sh/r14clb37j2b49uj/AACaDx4HUDOcHgJP25jznMqIa?dl=0&lst=>

- **Presentation**

Each group will give a short presentation of their project during the final, on **March 19th, 8am -11am**. It will be about 10 mins long plus 2 mins Q&A.

- **Final report**

Each group need to submit a single report on the project by **March 26th, 11:59 pm**. Ideally, the report should not exceed 5 pages, including figures (the lists of references are not counted). Please email your final report and the relevant source code to Prof. Kleinfeld (dk@physics.ucsd.edu). Remember to have your name and PID typed in the report.

W20 PHYS 178/278 Final Project Topics

1. Firing rates statistics of cortical neurons

On the distribution of firing rates in networks of cortical neurons. Roxin A, Brunel N, Hansel D, Mongillo G, van Vreeswijk C., J. Neurosci. (2011) 9;31(45):16217-26.

<https://doi.org/10.1523/JNEUROSCI.1677-11.2011>

The distribution of *in vivo* average firing rates within local cortical networks has been reported to be **highly skewed** and **long tailed**. The distribution of average single-cell inputs, conversely, is expected to be Gaussian by the central limit theorem. This raises the issue of how a skewed distribution of firing rates might result from a symmetric distribution of inputs. This article argues that skewed rate distributions are a signature of the nonlinearity of the *in vivo* $f-I$ curve. During *in vivo* conditions, ongoing synaptic activity produces significant fluctuations in the membrane potential of neurons, resulting in an expansive nonlinearity of the $f-I$ curve for low and moderate inputs.

Objective goals: investigate the effects of single-cell and network parameters on the shape of the $f-I$ curve and on the distribution of firing rates in randomly connected networks.

1. Analytical approach – deriving **the firing rate distribution**
Change sigma, Fig. 3A to 3C
Explore different mean firing rate, Fig. 4
2. Numerical approach – compute the firing rate distributions by simulating a *randomly connected network of integrate-and-fire neurons* (Fig. 5)

2. Emergent orientation selectivity from a *ring network model*

Theory of orientation tuning in visual cortex, BEN-YISHAI, R., LEV BAR-OR, R., Sompolinsky, H., *PNAS* 92:3844–3848 (1995). <https://doi.org/10.1073/pnas.92.9.3844>

The role of intrinsic cortical connections in processing sensory input and in generating behavioral output is poorly understood. This study examined this issue in the context of the tuning of neuronal responses in cortex to the orientation of a visual stimulus. They proposed a **ring network model** that incorporates both orientation-selective input from the lateral geniculate nucleus and orientation-specific cortical interactions. Depending on the model parameters, the network exhibits **orientation selectivity** that originates from within the cortex, by a symmetry-breaking mechanism. Based on the ring model, several experimental consequences of this cortical mechanism of orientation tuning are derived:

- The tuning width is relatively independent of the contrast and angular anisotropy of the visual stimulus.
- The transient population response to changing of the stimulus orientation exhibits a slow "virtual rotation."
- Neuronal cross-correlations exhibit long time tails, the sign of which depends on the preferred orientations of the cells and the stimulus orientation.

Objective goals: investigate different mechanisms for orientation selectivity in visual cortex by using a **ring network model**.

- Steady-state:
 - Derive the steady-state solution $M(\theta)$
 - Study the orientation tuning properties $M(\theta)$. How does **tuning width** θ_c of $M(\theta)$ depend on the **stimulus contrast** (c), and **anisotropy** (\mathcal{E}) for different ranges of values of the connectivity parameters?
- Time-dependent response:
 - Study the time-dependent response $m(\theta, t)$ to a change in the orientation of the external stimulus, and the cross-correlations (CCs) between the neurons in the network.

3. Generation of stable heading representations in diverse visual scenes

Generation of stable heading representations in diverse visual scenes. Kim S.S., Hermundstad A.M., Romani S, Abbott L.F., Jayaraman V. *Nature*. **576**(7785):126-31. (2019)
<https://doi.org/10.1038/s41586-019-1767-1>

Many animals rely on an internal heading representation when navigating in varied environments. How this representation is linked to the sensory cues that define different surroundings is unclear. In the fly brain, heading is represented by ‘**compass**’ **neurons** that innervate a ring-shaped structure known as the ellipsoid body. Each compass neuron receives inputs from ‘ring’ neurons that are selective for particular visual features; this combination provides an ideal substrate for the extraction of directional information from a visual scene.

Objective goals:

- Investigate the experimental observations regarding the ‘compass’ neurons of fly brain.
- Using the ring model provided in this article, run the simulation and study
 - how the correlated activity of compass and visual neurons drives plasticity, which flexibly transforms two-dimensional visual cues into a stable heading representation;
 - how network plasticity enables the flexible generation of a stable compass-neuron heading representation in different visual scenes.
- Try some of the untested ideas proposed in the Section “*Other aspects of plasticity rules to explore in the future*” in the SI texts.

[Supplementary information for simulation](#)

Simulation code - http://research.janelia.org/jayaraman/Kim_etal_Nature2019_Downloads/

4. Rhythmically neural control of breathing

Computational models of the neural control of breathing, Molkov, Y. I., Rubin, J. E., Rybak, I. A., Smith, J. C., *Rev Syst Biol Med.* 9:1–22 (2017). <https://doi.org/10.1002/wsbm.1371>

The ongoing process of breathing underlies the gas exchange essential for mammalian life. Each respiratory cycle ensues from the activity of rhythmic neural circuits in the brainstem, shaped by various modulatory signals, including mechanoreceptor feedback sensitive to lung inflation and chemoreceptor feedback dependent on gas composition in blood and tissues. This paper reviews a variety of computational models designed to reproduce experimental findings related to the neural control of breathing and generate predictions for future experimental testing. The review starts from the description of the core respiratory network in the brainstem, representing the central pattern generator (CPG) responsible for producing rhythmic respiratory activity, and progresses to encompass additional complexities needed to simulate different metabolic challenges, closed-loop feedback control including the lungs, and interactions between the respiratory and autonomic nervous systems. The integrated models considered in this review share a common framework including a distributed CPG core network responsible for generating the baseline three-phase pattern of rhythmic neural activity underlying normal breathing.

Objective goals:

Refer to the models discussed in this review, construct a mathematical model of **the respiratory central pattern generator (CPG)** that captures three neural activity ‘phases’ presence in the rhythmic motor pattern during normal breathing,

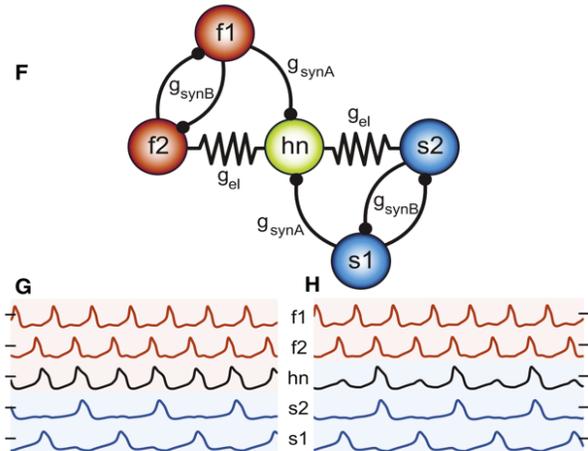
- inspiration (I),
- post-inspiration (post-I or P-I) or the first stage of expiration, and
- the later or second stage of expiration (called E-2),

Compare the simulations of your model with the existing experimental findings.

5. Competing rhythmic oscillators

Multiple mechanisms switch an electrically coupled, synaptically inhibited neuron between competing rhythmic oscillators, Gutierrez GJ, O'Leary T, Marder E, *Neuron* 77.5 (2013) <https://doi.org/10.1016/j.neuron.2013.01.016>

Rhythmic oscillations are common features of nervous systems. One of the fundamental questions posed by these rhythms is how individual neurons or groups of neurons are recruited into different network oscillations. More specifically, how are individual neurons or groups of neurons switched between, or recruited into, different oscillatory networks as a function of the strength of the electrical and chemical synapses in the network?



Objective goals:

Model a five-neuron circuit in which a hub neuron is connected to two different oscillatory subnetworks.

- Firstly, investigate the dynamics of each subunit of the five-neuron circuit (see Fig.1 B, C, D and E of the paper).
- Explore the patterns of coordination shown in the network as a function of the **electrical coupling** (g_{el}) and **inhibitory synapse** (g_{synA} , g_{synB}) strengths, and how the hub neuron can be switched between the fast and slow oscillators.

Three-dimensional parametrical space:

- The role of **electrical coupling** (g_{el}).
- The **inhibitory synaptic conductance** (g_{synA}) connecting to the hub neuron.
- The inhibitory synaptic conductance (g_{synB}) of half-center oscillators.

Quantify the activities of five neurons in terms of

- Spiking frequencies
- Phase relations

6. Coupled oscillators, modeling fish locomotion

The Nature of the Coupling Between Segmental Oscillators of the Lamprey Spinal Generator for Locomotion: A Mathematical Model, Cohen, A. H., Holmes, P. J., and Rand, R. H., *J. Math. Biology* 13:345–369 (1982). <https://doi.org/10.1007/BF00276069>

This study introduced a theoretical model which is used to explain the intersegmental coordination of the neural networks responsible for generating locomotion, i.e., swimming, in the isolated spinal cord of *lamprey*.



The electromyographic activity of the myotomal muscle of a fish exhibits a stereotyped temporal pattern. In spinal cord the ventral root (VR) output pattern underlying the muscle activity is believed to have three important features: (1) The activity of the two ventral roots of a single segment strictly alternates in time; (2) the duration of the activity of a VR is a constant proportion of the period of the cycle; (3) there is a delay between the bursts of any two ipsilateral ventral roots and that delay is proportional to the period (Fig 1.2).

Here, the model assumes that each segment of the cord consists of a pair of neural networks which can generate oscillatory activity. Pairs of oscillators (in ventral root) are assumed to be coupled together to form the central pattern generators (CPG) which then generates the complete stable pattern.

Objective goals:

Each segmental oscillator of spinal cord is approximated as a limit cycle oscillator which consists of only a single dependent variable, the phase $\theta(t)$. By considering set of N coupled limit cycle oscillators, demonstrate that,

- how stable phase locked motions which correspond to traveling waves in the spinal cord can be generated, thus simulating "fictive swimming";
- bidirectional coupling between the oscillators can generate a stable **traveling wave**.

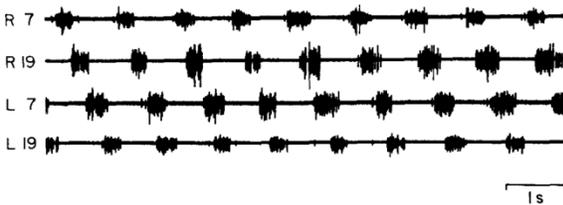


Fig. 1.2. Ventral root recordings from an isolated piece of spinal cord. Recordings are from the right and left roots of segments 7 and 19 (from Cohen and Wallén, 1980)

There is a delay between the bursts of any two ipsilateral ventral roots and that delay is proportional to the period. The third feature implies that the delay occupies a constant phase of the cycle, i.e. there is a constant phase coupling between the two segments.

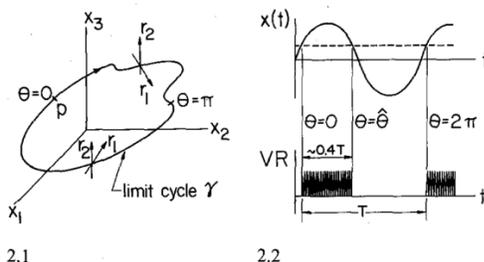


Fig. 2.1. The phase space of Eq. (2.1) in the special case $n = 3$, for which \mathbf{r} is a 2-vector, $\mathbf{r} = (r_1, r_2)$

Fig. 2.2. The oscillator output $x(t)$ and its relation to the ventral root output VR . The threshold level is shown as a dashed line

7. Oscillators with time-delayed coupling

Time-Delayed Spatial Patterns in a Two-Dimensional Array of Coupled

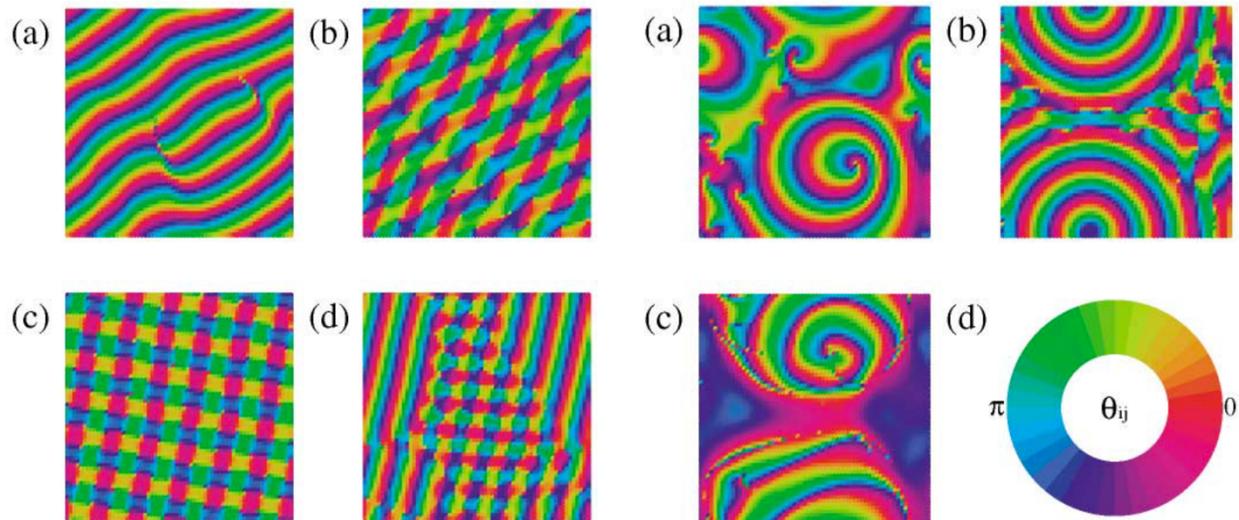
Oscillators, Jeong, S., Ko, T., Moon, H., *Phys. Rev. Lett.* 89 (15) (2002).

<https://doi.org/10.1103/PhysRevLett.89.154104>

Spatiotemporal patterns arise in numerous physical, chemical, and biological systems. The brain, one of the most complex systems, is now also known to generate spatiotemporal patterns such as plane waves and spirals. This study investigated the effects of **time-delayed** interactions in an ensemble of **two-dimensional coupled phase oscillators**. Each oscillator is allowed to interact with its neighbors located within a finite radius r_0 , and the coupling signal propagates at speed v .

Objective goals:

- Demonstrate that distance-dependent time delays induce various patterns including traveling rolls, square like and rhombus like patterns, spirals, and targets.
- Explore the parametrical space of **coupling length r_0** , **coupling coefficients K** , and **signal propagation speed v** . and analyze the stability boundaries between the synchronized planar solutions (when all oscillators are in the same phase) and the emerging patterns.



8. Propagating Neuronal Discharges in Neocortical Slices

Propagating Neuronal Discharges in Neocortical Slices: Computational and Experimental Study, Golomb D, Amitai Y., *J Neurophysiol.* 78(3):1199-211 (1997).

<https://doi.org/10.1152/jn.1997.78.3.1199>

When synaptic γ -aminobutyric acid-A (GABA_A) inhibition is pharmacologically suppressed in neocortical slices, neuronal population discharges¹ appear as responses to electrical stimulation above a certain strength. In extracellular recording, they are found to be abrupt, all-or-none field potentials (FPs). In intracellular recordings, they correspond to depolarizing shifts (DSs) in membrane potentials, above which rides a high-frequency train of action potentials. These discharges are referred to as “synchronous” or “epileptiform,” implying that adjacent cells tend to fire together.

Objective goals:

Based on the model of neocortical cells present in this study, construct a one-dimensional network with spatially decaying synaptic efficacies, and investigate the dynamic mechanisms that lead to the creation, propagation, and cessation of discharges. Specifically, seek the answers to the following questions:

- 1) What are the spatiotemporal properties of the discharge propagation, and how are they related to the network architecture?
- 2) How do the velocity and shape of the discharge depend on the synaptic parameters, such as the strength of AMPA and NMDA synaptic efficacies, and the level of synaptic depression?
- 3) What is the relationship between the propagation velocity and the synaptic kinetics?

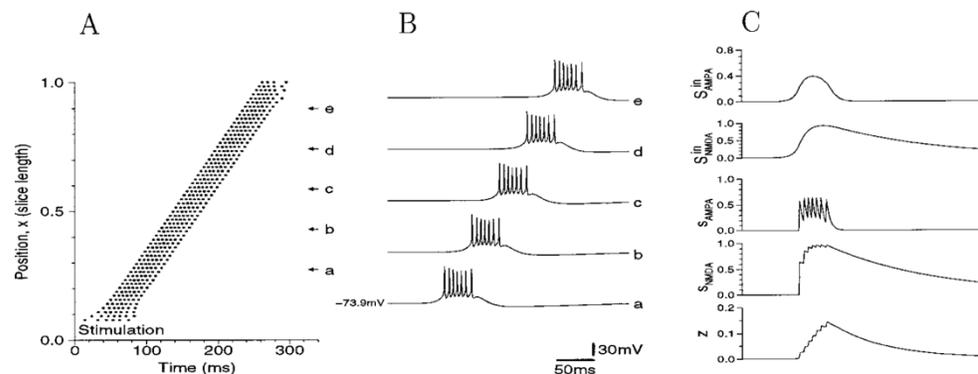


FIG. 3. Propagation of discharges in cortical slice model. There is no synaptic depression ($k_i = 0$), $g_{AMPA} = 0.31$ mS/cm², $g_{NMDA} = 0.25$ mS/cm². *A*: rastergram of excitatory cells. Only firing times from every 4th cell are shown. Arrows at *right*: position of 5 cells along slice whose voltage time courses are plotted in *B*. Initially cells at left ($x \leq 0.06$) are depolarized ($V = 10$ mV) and all others are at rest. Discharge propagates to *right* and far from edges maintains its shape; every neuron fires 7 spikes during discharge. *C*: time courses of internal variables of neuron denoted by *a*. From *top*: total AMPA and NMDA synaptic conductance, S_{AMPA}^{in} and S_{NMDA}^{in} , that this neuron receives (the neuron’s “input”); AMPA and NMDA auxiliary variables, S_{AMPA} and S_{NMDA} , of postsynaptic synapses connecting this neuron to others (the neuron’s “output”); slow potassium activation variable z . Auxiliary variables are normalized such that 1 means that all corresponding channels are open.

9. Recurrent neural integrator network model for horizontal eye position (line attractor)

Stability of the Memory of Eye Position in a Recurrent Network of Conductance-Based Model Neurons, Seung, H. Sebastian, et al., *Neuron* 26.1: 259-271 (2000).

[https://doi.org/10.1016/S0896-6273\(00\)81155-1](https://doi.org/10.1016/S0896-6273(00)81155-1)

Develop an oculomotor integrator model as a network of conductance-based neurons which interact with each other by recurring excitatory synapses. The integrator neurons receive feedforward inputs from three neurons. The vestibular neuron which is tonically active at a constant rate, simulating the background activity present in vestibular afferents when the head is stationary. The excitatory and inhibitory burst neurons that are normally silent, except for occasional brief burst of action potentials that cause saccadic eye movements. These bursts change the firing rates of neurons in the network which is maintained by recurrent excitation after the feedforward input is over. Signals from the integrator neurons lead to the oculomotor plant so that persistent changes in these signals cause persistent changes in the angular position of the eyes.

Objective goals:

This model should reproduce the following properties of biological integrator -

- Each integrator neuron in the model should exhibit a linear relationship between firing rate and eye position when it is active. However, there is also a threshold eye position below which it is silent. The linear slope and the threshold vary from neuron to neuron.
- Because of some imperfection in persistence, there is some drift of neural activity with time, which leads to drift in the eye position during fixation. The drift velocity depends systematically on eye position, generally in a nonlinear manner.
- The persistence of neural activity degrades when synaptic strengths are mistuned, neurons are destroyed, or the strength of feedback is otherwise perturbed.

10. Decision making

A Recurrent Network Mechanism of Time Integration in Perceptual Decisions

Wong, K.-F., Wang, X.-J., *J. Neurosci.* 26(4):1314-1328 (2006).

<https://doi.org/10.1523/JNEUROSCI.3733-05.2006>

Recent physiological studies using behaving monkeys revealed that, in a two-alternative forced-choice visual motion discrimination task, reaction time was correlated with ramping of spike activity of lateral intraparietal cortical neurons. The ramping activity appears to *reflect temporal accumulation*, on a timescale of hundreds of milliseconds, of sensory evidence before a decision is reached. In this paper, they adopt this reduced a biophysically based cortical microcircuit network model for decision making (Wang, 2002), to an **eleven-variable or two-variable version model** through mean-field approach.

Objective goals:

Understand the cortical circuit for decision making (Fig 1), and the re-derive the reduced version decision making model. With stability analysis and numerical simulation, try to investigate the following questions (you may use either **eleven-variable or two-variable** model for simulation depending on the questions):

- How does the recurrent dynamics give rise to a much longer integration time? Is this slow linear ramping a consequence of a network with slow recurrent excitation?
- Can the model still work when recurrent excitation is solely mediated by the much faster AMPA receptors (AMPA receptors)?
- Is it necessary that neurons subserving integration during stimulation also show persistent activity during working memory?

11. Dynamic gain control

Adaptation without parameter change: Dynamic gain control in motion detection, Borst, A., Flanagan, V. L., and Sompolinsky, H., *PNAS* 102(17): 6172-6176 (2005).

<https://doi.org/10.1073/pnas.0500491102>

Motion detection sensitive neuron of the fly visual system (H1) adapts its input-output relationship to changes in the statistics of the ambient stimulus. The rapid adaptation of the velocity response gain has been interpreted as evidence of optimal matching of the H1 response to the dynamic range of the stimulus, thereby maximizing its information transmission. Develop a motion detection model using Reichardt detectors, which extract the direction of motion by multiplying the brightness signals from neighboring image locations after asymmetric temporal filtering.

Objective goals:

The model should illustrate the following properties,

- Increasing the amplitude of the velocity fluctuations (variance) suppresses the contribution of the stimulus past, which leads to a marked reduction in the response gain.
- Increasing the stimulus variance shortens the time scale of the motion detection response thereby reducing it to the correlation time of the stimulus fluctuations.

As we know that nervous system is inherently nonlinear and multidimensional, develop a simple neuron model which shows that changing the form of nonlinearity may have significant effects on the magnitude of the resultant adaptive response.

12. Hebbian learning rule

Spike-Timing-Dependent Hebbian Plasticity as Temporal Difference Learning **Competitive Hebbian learning through spike-timing-dependent synaptic plasticity (STDP)**, Song, S., Miller, K. D., Abbott, L. F., *Nat. Neurosci.* 3 (9): 919-926 (2000).

<https://doi.org/10.1038/78829>

A spike-timing-dependent Hebbian mechanism governs the plasticity of recurrent excitatory synapses in the neocortex: synapses that are activated a few milliseconds before a postsynaptic spike are potentiated, while those that are activated a few milliseconds after are depressed. We show that such a mechanism can implement a form of **temporal difference learning for prediction of input sequences**. Using a biophysical model of a cortical neuron, this paper shows that a temporal difference rule used in conjunction with dendritic backpropagating action potentials reproduces the temporally asymmetric window of Hebbian plasticity observed physiologically. Furthermore, the size and shape of the window vary with the distance of the synapse from the soma. This work shows how a spike-timing-based temporal difference learning rule can allow a network of neocortical neurons to predict an input a few milliseconds before the input's expected arrival.

Objective goals:

Reproduce the paper's simulation: model the balanced excitation network with LIF neurons ($n = 1000$). The (excitation) synapses are updated by STDP modification rule.

- 1) Given different mean presynaptic input rates (stochastic presynaptic spike trains), what is the
 - (a) equilibrium distribution of synaptic strengths arising from STDP;
 - (b) the spiking variability, i.e., coefficient of variation (CV) of the postsynaptic spike train.
- 2) **Latency reduction:** given the presynaptic inputs are correlated in various ways, how does the latency between post- and presynaptic spikes change, before and after the synaptic strengths are learned (and stable) through the STDP rule.

13. Coincidence detection – a building block model for sound localization

Simple models show the general advantages of dendrites in coincidence detection, Dasika, V. K., White, J. A. & Colburn, H. S., *J. Neurophysiol.* 98(5): 3449 (2007). <https://doi.org/10.1152/jn.00669.2005>

Simple models are used to elucidate mechanisms underlying the dendritic enhancement of coincidence detection. This paper focus on coincidence-detecting cells in the auditory system, which have bipolar dendrites and show acute sensitivity to **interaural time difference (ITD)**, a critical cue for spatial hearing.

Builds a model cell that consists of a single-compartment soma with two identical passive dendritic sections attached to the soma, where each dendritic section is composed of a single dendritic-compartment or either a finite number or an infinite number (i.e., a cable) of compartments.

Objective goals:

Based on the model neuron, identify the fundamental mechanisms that underlie the dendritic improvement of **coincidence detection**.

1) Constant-conductance inputs

How does the soma response change with different dendritic conductance for the two dendritic sections, each of which has either single-, multiple-, or infinite- dendritic compartments?

2) Dynamic inputs (Paired-pulse inputs)

The precision/accuracy to detect coincidence depends on **a) the timing** and **b) the width of action potential** that triggers the presynaptic neuron to release neurotransmitters (let the waveform of potential is a pulse with a finite width), **c) the difference between two dendritic lengths** of postsynaptic neuron. Investigate how the three factors affect the coincidence sensitivity.

*The synaptic transmission can be model with the opening-closing dynamics of Ca^{2+} channels.

Other refs: <http://gureckislab.org/courses/spring13/robots/SoundLocalization-5.html>

14. Neuronal spike trains data analysis

Analysis of Neuronal Spike Trains, Deconstructed, Aljadeff, J., Lansdell, B. J., Fairhall, A. L., & Kleinfeld, D., *Neuron*, 91(2), 221–259 (2016).

<https://doi.org/10.1016/j.neuron.2016.05.039>

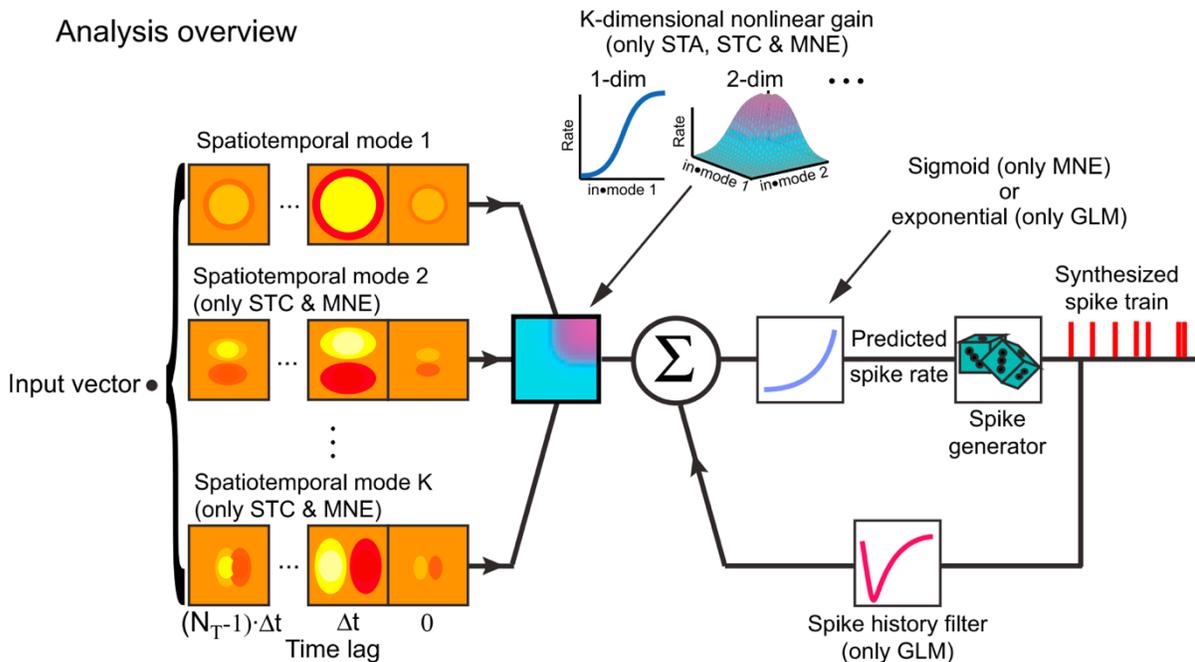
As information flows through the brain, neuronal firing progresses from encoding the world as sensed by the animal to driving the motor output of subsequent behavior. One of the more tractable goals of quantitative neuroscience is to develop predictive models that relate the sensory or motor streams with neuronal firing.

Objective goals:

Based on the statistics of applied stimuli (uncorrelated or correlated), select the proper analysis approaches to analyze the spike trains and extracting the relevant stimuli features.

- Spike-triggered average (STA)
- Spike-Triggered Covariance (STC)
- Maximum Noise Entropy Method (MNE)
- Generalized Linear Models (GLM)

The group can use the dataset acquired from their research project or search the available dataset online. Dataset and accompanying code presented in the paper is also available (<https://github.com/NeuroInfoPrimer/primer>).



15. Topological data analysis in natural odor statistics

Hyperbolic geometry of the olfactory space. Zhou Y, Brian H. Smith B. H., Sharpee T. O., *Sci Adv.* 4(8):eaag1458 (2018) <https://doi.org/10.1126/sciadv.aag1458>

In the natural environment, the sense of smell, or olfaction, serves to detect toxins and judge nutritional content by taking advantage of the associations between compounds as they are created in biochemical reactions. This suggests that the nervous system can classify odors based on statistics of their co-occurrence within natural mixtures rather than from the chemical structures of the ligands themselves. We show that this statistical perspective makes it possible to map odors to points in a hyperbolic space. Hyperbolic coordinates have a long but often underappreciated history of relevance to biology. For example, these coordinates approximate the distance between species computed along dendrograms and, more generally, between points within hierarchical tree-like networks.

Objective goals:

0. Read Giustia C, Itskov V, *Clique topology reveals intrinsic geometric structure in neural correlations*, 2015
1. Given odor concentration matrix, compute the N-by-N pairwise correlation matrix and its first 3 Betti curves.
2. Generate Betti curves by randomly sampling N points in Euclidean unit cube of different dimensions (repeat 100 times), and compare them to the Betti curves obtained in the first step.
3. Generate Betti curves by randomly sampling N points in 3D Hyperbolic space of different Rmax (repeat 100 times), and compare them to the Betti curves obtained in the first step.
4. (Optional) Embed pairwise correlation into the identified geometric space.

16. Analysis of Neuronal Morphology

Maximization of the connectivity repertoire as a statistical principle governing the shapes of dendritic arbors, Wen, Q., Stepanyants, A., Elston, G. N., Grosberg, A.Y, and Chklovskii, D. B., *PNAS*, 106 (30) 12536-12541 (2009)

<https://doi.org/10.1073/pnas.0901530106>

The shapes of dendritic arbors are fascinating and important, yet the principles underlying these complex and diverse structures remain unclear. Wen et al. analyzed basal dendritic arbors of 2,171 pyramidal neurons sampled from mammalian brains and discovered three statistical properties:

1. the dendritic arbor size scales with the total dendritic length,
2. the spatial correlation of dendritic branches within an arbor has a universal functional form,
3. and small parts of an arbor are self-similar.

Wen et al. proposed that these properties result from *maximizing the repertoire of possible connectivity patterns between dendrites and surrounding axons while keeping the cost of dendrites low*. They solved this optimization problem by drawing an analogy with *maximization of the entropy* for a given energy in statistical physics. The solution is consistent with the above observations and predicts scaling relations that can be tested experimentally.

Objective goals:

- Scaling, universality, and self-similarity (Eq. 1) of basal dendritic arbors of pyramidal neurons.
- Derived an analytical expression for connectivity repertoire (Eq. 2), and dendritic cost.
- Maximizing the connectivity repertoire for a given dendritic cost and compared the results with experimental measurements.

17. Bring up the topic that interests you

You are welcome to find a topic that you are interested in or relevant to your on-going research.